

13

```
> #2.  
> Kidney <- read.csv("Kidney_Function_Data.csv", header = F)  
> colnames(Kidney) <- c("Y", "X1", "X2", "X3")  
> #2.(a)  
> x1 <- Kidney$X1 - mean(Kidney$X1)  
> x2 <- Kidney$X2 - mean(Kidney$X2)  
> x3 <- Kidney$X3 - mean(Kidney$X3)  
> Kidney.lm <- lm(Y~x1*x2*x3, data = Kidney)  
> Kidney.lm
```

Call:

```
lm(formula = Y ~ x1 * x2 * x3, data = Kidney)
```

Coefficients:

(Intercept)	x1	x2
82.66306	-45.10057	-0.74429
x3	x1:x2	x1:x3
0.95737	0.74158	0.36246
x2:x3	x1:x2:x3	
-0.01617	-0.03316	

```
> #Yi = 82.663.6 -45.10057Xi1 -  
0.74429Xi2+0.95737Xi3+30.74158Xi1Xi2+0.36246Xi1Xi3-0.01617Xi2Xi3-  
0.03316Xi1Xi2Xi3 +residul_i  
>  
> Kidney.lm2 <- lm(Y ~ x1*x2*x3 + poly(x1, 2) + poly(x2, 2) + poly(x3, 2), data =  
Kidney)  
> Kidney.lm2
```

Call:

```
lm(formula = Y ~ x1 * x2 * x3 + poly(x1, 2) + poly(x2, 2) + poly(x3,  
2), data = Kidney)
```

Coefficients:

(Intercept)	x1	x2
84.09757	-45.00064	-0.72517
x3	poly(x1, 2)1	poly(x1, 2)2
1.01668	NA	11.72818

```

poly(x2, 2)1  poly(x2, 2)2  poly(x3, 2)1
              NA           14.24919           NA
poly(x3, 2)2           x1:x2           x1:x3
-17.89652           0.31876           0.44109
              x2:x3           x1:x2:x3
-0.02136           -0.05720

>
> library("ALSM")
> library("leaps")
> BestSub(Kidney[, 2:4], Kidney[, 1], method = 'aic', num = 3)
  p 1 2 3      SSEp      r2      r2.adj
1 2 1 0 0 11068.478 0.6429007 0.63138133
1 2 0 1 0 17169.856 0.4460535 0.42818429
1 2 0 0 1 27286.682 0.1196571 0.09125894
2 3 1 1 0  7666.102 0.7526706 0.73618198
2 3 1 0 1  8713.158 0.7188897 0.70014903
2 3 0 1 1 12393.018 0.6001674 0.57351187
3 4 1 1 1  4499.974 0.8548186 0.83979979
      Cp      AICp      SBCp      PRESSp
1  42.33061 195.9065 198.8995 12402.603
1  81.65083 210.3953 213.3883 19676.109
1 146.84854 225.6823 228.6753 30198.308
2  22.40406 185.7858 190.2754  9348.907
2  29.15179 190.0107 194.5002 10326.342
2  52.86659 201.6366 206.1261 14864.376
3   4.00000 170.2055 176.1916  5963.853
> #subset      AIC
> #x1,x2,x3    170.2055
> #x1,x2      185.7858
> #x1,x3      190.0107
>
> #2.(b)
> #Not so much at all
>
> #3.
> PA <- read.csv("Performance_Ability_Data.csv", header = F)
> colnames(PA) <- c("Y", "X")

```

```
> PA
  Y  X
1 0 474
2 0 432
3 0 453
4 1 481
5 1 619
6 0 584
7 0 399
8 1 582
9 1 638
10 1 624
11 1 542
12 1 650
13 1 553
14 0 425
15 1 563
16 0 549
17 1 498
18 0 520
19 1 610
20 0 598
21 0 491
22 0 617
23 1 621
24 0 573
25 1 562
26 0 506
27 1 600
> #3.(a)
> PA.glm <- glm(Y ~ X,
+               data = PA, family = "binomial")
> PA.glm
```

Call: `glm(formula = Y ~ X, family = "binomial", data = PA)`

Coefficients:

(Intercept)                    X

-10.30893      0.01892

Degrees of Freedom: 26 Total (i.e. Null); 25 Residual

Null Deviance: 37.39

Residual Deviance: 29.24      AIC: 33.24

> #odds = exp(-10.30893+0.01892X)

> #3.(b)

> plot(PA\$X, as.integer(PA\$Y)-1)

> lines(lowess(PA\$X, as.integer(PA\$Y)-1),

+      col = 2, lwd = 2, lty = 2)

>

> a <- min(PA\$X)

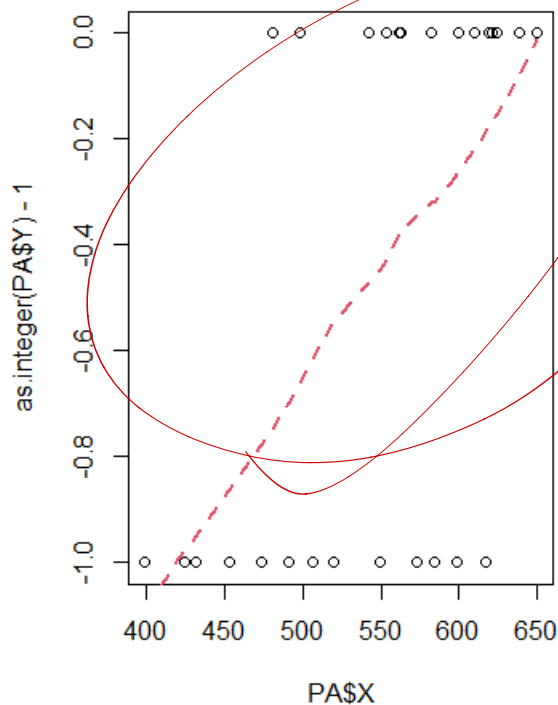
> b <- max(PA\$X)

> new.X <- data.frame(X = seq(a, b, len = 50))

> predicted.Y <- predict(PA.glm, new.X, type="response")

> new.X <- c(new.X)\$X

> lines(new.X, predicted.Y, lwd = 2, col = "black")



> #2.

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```

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> x3 <- Kidney$X3 - mean(Kidney$X3)
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> Kidney.lm2 <- lm(Y ~ x1*x2*x3 + poly(x1, 2) + poly(x2, 2) + poly(x3, 2), data =
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poly(x2, 2)1	poly(x2, 2)2	poly(x3, 2)1
NA	14.24919	NA
poly(x3, 2)2	x1:x2	x1:x3

-17.89652	0.31876	0.44109
x2:x3	x1:x2:x3	
-0.02136	-0.05720	

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> colnames(PA) <- c("Y", "X")
> PA
  Y  X
1 0 474

```

```
2 0.432
3 0.453
4 1.481
5 1.619
6 0.584
7 0.399
8 1.582
9 1.638
10 1.624
11 1.542
12 1.650
13 1.553
14 0.425
15 1.563
16 0.549
17 1.498
18 0.520
19 1.610
20 0.598
21 0.491
22 0.617
23 1.621
24 0.573
25 1.562
26 0.506
27 1.600
```

```
> #3.(a)
```

```
> PA.glm <- glm(Y ~ X,
+               data = PA, family = "binomial")
> PA.glm
```

```
Call: glm(formula = Y ~ X, family = "binomial", data = PA)
```

```
Coefficients:
```

```
(Intercept)          X
-10.30893         0.01892
```

```
Degrees of Freedom: 26 Total (i.e. Null); 25 Residual
```

```

Null Deviance:    37.39
Residual Deviance: 29.24    AIC: 33.24
> #odds = exp(-10.30893+0.01892X)
> #3.(b)
> plot(PA$X, as.integer(PA$Y)-1)
> lines(lowess(PA$X, as.integer(PA$Y)-1),
+       col = 2, lwd = 2, lty = 2)
>
> a <- min(PA$X)
> b <- max(PA$X)
> new.X <- data.frame(X = seq(a, b, len = 50))
> predicted.Y <- predict(PA.glm, new.X, type="response")
> new.X <- c(new.X)$X
> lines(new.X, predicted.Y, lwd = 2, col = "black")
> #3.(c)
> summary(PA.glm)

```

Call:

```
glm(formula = Y ~ X, family = "binomial", data = PA)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-1.7845	-0.8350	0.5065	0.8371	1.7145

Coefficients:

	Estimate	Std. Error	z value
(Intercept)	-10.308925	4.376997	-2.355
X	0.018920	0.007877	2.402

Pr(>|z|)

(Intercept)	0.0185 *
X	0.0163 *

---

Signif. codes:

0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 37.393 on 26 degrees of freedom



Residual deviance: 29.242 on 25 degrees of freedom  
AIC: 33.242

Number of Fisher Scoring iterations: 4

~~> #3(c)  
> summary(PA.glm)~~

Call:  
glm(formula = Y ~ X, family = "binomial", data = PA)

Deviance Residuals:

Min	1Q	Median	3Q	Max
-1.7845	-0.8350	0.5065	0.8371	1.7145

Coefficients:

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(Dispersion parameter for binomial family taken to be 1)

Null deviance: 37.393 on 26 degrees of freedom  
Residual deviance: 29.242 on 25 degrees of freedom  
AIC: 33.242

Number of Fisher Scoring iterations: 4

> #b1 = 0.018920  
> exp(b1)  
Error: object 'b1' not found  
> b1 = 0.018920

```

> exp(b1)
[1] 1.0191
> #3.(d)
> predicted.Y <- predict(PA.glm, 550, type="response")
Error in model.frame.default(Terms, newdata, na.action = na.action, xlev =
object$xlevels) :
  'data' must be a data.frame, environment, or list
> #3.(d)
> data.frame(550)
  X550
1  550
> predicted.Y <- predict(PA.glm,new.X , type="response")
Error in model.frame.default(Terms, newdata, na.action = na.action, xlev =
object$xlevels) :
  'data' must be a data.frame, environment, or list
> new.X <- data.frame(MonthExperience = seq(a, b, len = 50))
> new.X
  MonthExperience
1          399.0000
2          404.1224
3          409.2449
4          414.3673
5          419.4898
6          424.6122
7          429.7347
8          434.8571
9          439.9796
10         445.1020
11         450.2245
12         455.3469
13         460.4694
14         465.5918
15         470.7143
16         475.8367
17         480.9592
18         486.0816
19         491.2041
20         496.3265

```

```
21      501.4490
22      506.5714
23      511.6939
24      516.8163
25      521.9388
26      527.0612
27      532.1837
28      537.3061
29      542.4286
30      547.5510
31      552.6735
32      557.7959
33      562.9184
34      568.0408
35      573.1633
36      578.2857
37      583.4082
38      588.5306
39      593.6531
40      598.7755
41      603.8980
42      609.0204
43      614.1429
44      619.2653
45      624.3878
46      629.5102
47      634.6327
48      639.7551
49      644.8776
50      650.0000
```

```
> #3.(c)
```

```
> summary(PA.glm)
```

Call:

```
glm(formula = Y ~ X, family = "binomial", data = PA)
```

Deviance Residuals:

```
      Min       1Q   Median       3Q      Max
```

-1.7845 -0.8350 0.5065 0.8371 1.7145

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X	0.018920	0.007877	2.402	
	Pr(> z )			
(Intercept)	0.0185 *			
X	0.0163 *			

---

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> b1 = 0.018920  
> exp(b1)  
[1] 1.0191  
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> #3.(d)  
> new.X <- data.frame(550)  
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```