

1.(25%)(配分：5%/小題, 觀念對表達怪 3)

(a)對資料收集、整理、分析、預測，給出正確訊息之科學

(b)由表格、圖形或數字來描繪或總結數據的方法

(c)從樣本獲得的數據對母體參數進行估計和假設的方法

(d)在某些條件下多組數據於分組討論時滿足某一性質，但數據合併討論時卻可能得到相反結論的現象

(e)兩變數間線性相關的測量參數

2.(40%)(配分：8%/小題，多寫扣1%)

(a) nominal, ordinal, interval, ratio (2%/per)

(b) bar chart, pie chart. (4%/per)

(c) determine the number of nonoverlapping classes,

the width of each class and the class limits (3%+3%+2%)

(d) dot plot, histogram, stem&leaf display, box plot (2%/per)

(e) mean:  $\frac{1}{n} \sum_{i=1}^n X_i$

weighted mean:  $\frac{\sum_{i=1}^n W_i X_i}{\sum_{i=1}^n W_i}$

median: For an odd number of observations, the median is the middle value

For an even number of observations , the median is the average of the two middle values

geometric mean:  $\sqrt[n]{X_1 \dots X_n}$

mode: The mode of a data set is the value that occurs with greatest frequency

percentiles:  $L_p = \frac{p}{100}(n + 1) = a + b, a \in \mathbb{N}, 0 \leq b < 1$

$\eta_p = \#a + b * (\#(a + 1) - \#a)$

配分 : (2%+1%+1%+1%+1%+2%)

3.(15%)(配分 : 5%/小題)

(a)batting average of Fealey when she' s junior(**senior**) is .375(**.3**)

And Janson' s is .35(**.292**)

In this analysis, Fealey with higher batting average whenever she is junior or senior should be awarded the scholarship.

(b) batting average of Fealey is .310, and Janson' s is .328

In this analysis, Jason with higher batting average should be awarded the scholarship.

(c)No , because we ignore the influence of another variable , this is called Simpson's Paradox

4.(20%)(配分 : 10%/小題)

(a)75%

(b)95% , higher

Because we have stronger conditions (the distribution is symmetric), we can guarantee that more data will be within two standard deviations, using empirical rule

5.(加分 10%)

Let  $h(t)=E[(X - \mu_x) + t(Y - \mu_y)]^2 = E(X - \mu_x)^2 + 2tE[(X - \mu_x)(Y - \mu_y)] + E(Y - \mu_y)^2 \geq 0, \forall t \in \mathcal{R}$

$$\therefore \Delta = 4t^2 [E(X - \mu_x)(Y - \mu_y)]^2 - 4E(X - \mu_x)^2 E(Y - \mu_y)^2 \leq 0$$

$$\Rightarrow E(X - \mu_x)^2 E(Y - \mu_y)^2 \geq [E(X - \mu_x)(Y - \mu_y)]^2$$

$$\therefore \text{Var}(X)\text{Var}(Y) \geq [\text{Cov}(X, Y)]^2$$

$$\Rightarrow 1 \geq \frac{[\text{Cov}(X, Y)]^2}{\sigma_x \sigma_y} = \rho_{X,Y}^2$$

$$\therefore -1 \leq \rho_{X,Y} \leq 1$$